Information Retrieval WS 2016 / 2017

Lecture 3, Tuesday November 8th, 2016 (Efficient List Intersection)

> Prof. Dr. Hannah Bast Chair of Algorithms and Data Structures Department of Computer Science University of Freiburg

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Overview of this lecture

- Organizational
 - Your experiences with ES 2
 - About the tutorials
- Contents
 - List Intersection Recap, Time Measurement
 - Non-algorithmic improvements Arrays, Branching, Sentinels
 - Algorithmic improvements Galloping Search, Skip Pointers

Exercise Sheet 3: implement list intersection and make it as fast as possible on a small benchmark we have prepared

Ranking and Evaluation

Online vs. Personal

Experiences with ES2 1/3

Summary / excerpts

- Time-extensive exercise sheet, but again mostly due to lack of programming experience or practice
- Some mistakes in the TIP file, but quickly fixed when pointed out on the forum

Please always watch the forum for updates !

- Some problems with the floats (1.885) in the test cases
- Some bugs not found by test cases
- Lecture recording helped a lot
- One does not program well with: a cold, lack of sleep, lack of concentration, starting late, ...

Experiences with ES2 2/3

Results

Small differences in the implementation can make a significant difference in the results

- Variation of the BM25 parameters make some queries better, but don't affect others or make them worse
- Boosting (popular documents, full match) helped a bit
- Removing frequent words ("stop words") helped a bit
- Best results: $P@3 \approx 60\%$, $P@R \approx 40\%$, MAP $\approx 40\%$
- Bottom line: tuning a ranking algorithm is super important (for result quality) but also super hard

In particular, it is very hard to understand / predict the effect of changes in the parameters / implementation

Experiences with ES2 3/3

Test Cases

 A working program written by yourself is a confirmation that you have really understood the stuff from the lecture However: this only holds true if the program does what it should do and not just "something"

Experience from (many) previous courses: a significant fraction of students submit code that technically "works" but is otherwise wrong or even completely wrong

E.g. for ES2, a completely wrong ranking

 This is why we make the effort to provide test cases for you and require from you that you implement them

This has actually been a frequent request in previous years

Tutorials

Online vs. personal

- So far, the tutorials are completely online:

You submit online, you get feedback online, and questions and answers are online

- This is great because it gives you a lot of flexibility (you can work and ask any time you prefer)
- However, some people prefer a personal meeting, at least from time to time ... hence we offer:

You can meet with your tutor anytime, just ask him/her

There will be a personal tutorial every four weeks or so

QUESTION: when would be a good time for you?

Recap and motivation for today

- In Lecture 1, we have intersected the inverted lists
- In Lecture 2, we have merged the inverted lists
- For efficiency reasons, many search engines only return results which contain all the query words

Apache's Lucene, the most widely used open-source search engine, supports intersect (AND) and merge (OR) In most applications, intersect is used by default

Today we will focus on **efficiency** and therefore on list intersection

List Intersection 2/4

Time measurement

 Trickier than it may seem at first, because there can be significant variation between runs, for example due to: Other jobs running on your machine

The Java garbage collector running unpredictably

Data is partly in disk cache / L1-cache / TLB cache

 Therefore, always repeat your time measurements, and take the average over all these

For ES3, repeat 5 times for each measurement

Note: repetition itself can also distort the truth because of caching effects ... but not an issue for us today List Intersection 3/4

Time measurement in Java

- For millisecond resolution

long time1 = System.currentTimeMillis();
// whatever code you want to time
long time2 = System.currentTimeMillis();
long millis = time2 - time1;

- For microsecond resolution

long time1 = System.nanoTime();
// whatever code you want to time
long time2 = System.nanoTime();
long micros = (time2 - time1) / 1000;

■ Time measurement in **C++**

– For millisecond resolution (C-Style) #include <time.h>

clock_t time1 = clock();

// whatever code you want to time
clock_t time2 = clock();

size_t millis = 1000 * (time2 - time1) / CLOCKS_PER_SEC;

Motivation

 Implementation details can have a great impact on performance (even with the same underlying algorithm)

- Let us implement the basic "zipper" algorithm for list intersection from Lecture 1 and look at a few variations
- We make a part of the code (reading from file and the basic algorithm) available to you in both Java and C++

This should make ES3 easier / less work for you

- During the lecture, I will implement in Java today

Note that using **Python** makes little sense when studying efficiency issues: the overhead of its internal data types (i.p. Python's lists/arrays) weighs too heavy

Native arrays

 Java: ArrayList much worse than native [] array
 Elements of an ArrayList cannot be basic data types (e.g. int), but have to be objects (e.g. Integer)

This causes inefficient byte code / machine code

- C++: std::vector is as good as [] with option -O3

Elements of an std::vector can be basic data types as well as objects

Due to C++'s templating mechanism, machine code for std::vector<int> is almost the same as for int[]

Predictable branches

- Branches = all conditional parts in your code

In particular, **if ... then ... else** parts

- Modern processors do pipelining = speculative execution of future instructions before the current ones are done
- For conditional parts they have to guess the outcome
- So good to **minimize** amount of conditional parts and/or improve the predictability of conditionals

A conditional has good predictability if it evaluates to the same Boolean value most of the time

Sentinels

Special elements to avoid testing for index out of bound
 Less code + further reduction in number of branches

ZW

- For list intersection: id ∞ at the end of both lists
 - For Java, take: Integer.MAX_VALUE
 - For C++, take: std::numeric_limits<int>::max()

Algorithmic improvements 1/8

Preliminaries

- We have two lists, which we want to intersect
- Let **A** be the smaller list, with **k** elements
- Let **B** be the longer list, with **n** elements

List intersection is commutative, so we can always assume that the first list is A, and the second is B

 Recall that both lists are **sorted** ... this is crucial for the basic algorithm and all the algorithms in the following Algorithmic improvements 2/8

Binary search in the longer list

– Search each element from A in B, using binary search

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– This has time complexity $\Theta(k \cdot \log n)$

Good for small k ... but for $k = \Theta(n)$ this is $\Theta(n \cdot \log n)$, and hence slower than the "zipper"-style linear intersect

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Algorithmic improvements 3/8

Binary search in remainder of longer list

- Time complexity in the best case $\Theta(k + \log n)$ First element from A towards the end of list B
- Time complexity in the worst case $\Theta(k \cdot \log n)$ All elements of A at the beginning of list B



- Time complexity in the "typical" case $\Theta(k \cdot \log n)$ Elements of A "evenly distributed" over list B

Galloping search

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- Goal: when elements A[i] and A[i+1] are located at positions j₁ and j₂ in B, then, with d:= j₂ j₁ ("gap"): spend only time O(log d) to locate element A[i+1]
- Idea: first do an exponential search, to get an upper bound on the range, then a binary search as before





Algorithmic improvements 6/8

Proof of Lemma ... max $\Sigma_i \ln d_i$ under constraint $\Sigma_i d_i \le n$

- This is an instance of **Lagrangian optimization**:
 - 1. Write constraint as equation: $\Sigma_i d_i n' = 0 \dots n' < n$
 - 2. Define $\mathbf{L}(\mathbf{d_{1'}}, ..., \mathbf{d_{k'}} \boldsymbol{\lambda}) = \Sigma_i \ln d_i \neq \lambda \cdot (\Sigma_i d_i n')$
 - 3. Set partial derivatives = 0 to find all local optima and check the objective function at the borders

$$\frac{\partial L}{\partial d_i} = \frac{1}{d_i} - \Lambda \stackrel{!}{=} O \implies d_i = \frac{1}{\lambda}$$

$$\implies d_i \text{ one all equal (*)}$$

$$\frac{\partial L}{\partial d_{i}^{2}} = -\frac{1}{d_{0}^{2}} \leq 0 \quad = \text{ we have a MAX ad } d_{i} = \frac{1}{A}.$$

$$(*) = d_{i} = \frac{m!}{2} = \int_{i=1}^{2} \log d_{i} \leq \sum_{j=1}^{2} \log \frac{m!}{2} \leq 2 \cdot \log \frac{m}{2} \equiv 1$$

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Comparison-based lower bound

- Recall the lower-bound for comparison-based sorting
 There are n! possible outputs, we have to differentiate between all of them, and only two choices per step
 Hence #steps required ≥ log₂ (n!) = Ω(n · log n)
- We can use a similar argument for intersection / union:

There are n+k over k ways how the k elements from A can be placed within the n elements from B, ...

Hence #steps required $\geq \log_2 (n/k)^k = \mathbf{k} \cdot \log_2 (n/k)$

Galloping search is hence asymptotically optimal



- Idea: potentially skip large parts of longer list B
- Skip pointer = special element in list B with a value x and the index j of the first element in B with $B[j] \ge x$

When intersecting, follow pointer if current $A[i] \ge x$

Placement of skip pointers is heuristic ... for ES3 you can investigate good placements experimentally

– Advantage: **very simple** to implement

In particular, simpler than galloping search and thus often more effective in practice, even if not "optimal"

References

Textbook

Section 2.3: Faster intersection with skip pointers

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Literature

A simple algorithm for merging two linearly ordered setsF.K. Hwang and S. LinSICOMP 1(1):31–39, 1980A fast set intersection algorithm for sorted sequencesR. Baeza-YatesCPM, LNCS 3109, 31–39, 2004

Wikipedia

http://en.wikipedia.org/wiki/Lagrange multiplier